## **REVISED EDITION**

# MATHEMATICS IN THE MODERN WORLD

A CHED GENERAL EDUCATION CURRICULUM COMPLIANT

Winston S. Sirug, Ph.D.



ΑΒΧΔΕΓΗΙθΚΛΜΝΟΠΘΡΣΤΥςΩΑΒΧΔΕΓΗΙθΚΛΜΝΟΠΘΡΣΤΥςΩ

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A WSS Senior High School Book Series

Winston S. Sirug, Ph.D. Full Professor

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